Math 1314 Section: $\qquad$

## Lab 3 Chapter 3

Name: $\qquad$
Please show all work in the space provided for credit.
1.) The equation $y=-657.095 x^{2}+2859.214 x+12109.167$ models the sales of $R V$ 's (recreational vehicles) in millions of dollars ( $y$ ) from 2003 to 2009. " $x$ " is the number of years past 2003. ( $y=1,234$ means $\$ 1,234,000,000$ )
a.) Algebraically, find the year in which the sales for $R V$ 's was at its maximum. Use $x=-b / 2 a$ formula. Show work.

Find the year: $\qquad$
b.) What were the maximum RV sales in that year? (Notice units) \$ $\qquad$
2. For $g(x)=3 x^{2}-12 x+6$, answer the following questions.
a. Find the x -intercepts. Show work.
b. State the coordinates of the $y$-intercept. $\qquad$
c. State the vertex. $\qquad$
d. State the axis of symmetry.
e. State the direction of the parabola (opening up or down) $\qquad$
f. Decide whether there is a relative maximum or minimum, then state it. $\qquad$
g. Graph the function accurately using the above information.


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3. Given a cubic polynomial function $p(x)=a x^{3}+b x^{2}+c x+d,(a, b, c, d \neq 0)$, answer the following questions. Justify each answer.
a. How many $x$-intercepts can there be? $\qquad$
b. Does the degree of this polynomial function guarantee any $x$-intercepts? $\qquad$
c. Will the graph pass through the origin? $\qquad$
d. Could the graph "touch" the x-axis in two different places? $\qquad$
e. Identify the end behavior of the graph. $\qquad$
f. If it is known that one zero is real and another zero is imaginary, what can be determined about the remaining zeros?
4.) The function $f(x)=\frac{6.5 x^{2}-20.4 x+234}{x^{2}+36}$ models the pH level, $f(x)$ of the human mouth $x$ minutes after a person eats food containing sugar.
a. Determine to the nearest tenth the pH level of the human mouth 42 minutes after a person eats food containing sugar.
b. What is the equation of the horizontal asymptote associated with this function?
5.) For the function $f(x)=6 x^{4}-41 x^{3}+78 x^{2}-9 x-54$,
a. State the degree of the polynomial.
b. Use the Rational Zero Theorem to list all of the possible rational zeros.
c. Use a graphing calculator to determine which numbers in the list of possible rational zeros are probable rational zeros (indicated by the x-intercepts of the graph).

The graph appears to cross the $x$-axis at how many x-intercepts?
The graph appears to touch the $x$-axis at how many $x$-intercepts?
$\qquad$
d. Use synthetic division and then other algebraic methods to find all the zeros.

## Zeros:

